

reduced mass

$$\mu = \frac{mM}{m+M}$$

$$\alpha_{\text{EM}} = \frac{e^2}{4\pi\epsilon_0\hbar c} = \frac{1}{137.036\dots}$$

$$R_y = \alpha_{\text{EM}}^2 \cdot \frac{m_e c^2}{2} = 13.606\dots \text{eV}$$

Rydberg

$$a_0 = \frac{\hbar}{\alpha_{\text{EM}} m_e c} = 0.053\dots \text{nm}$$

Bohr radius

$$E_{n,l,m} = -R_y \frac{Z^2}{n^2} \cdot \frac{\mu}{m_e}$$

$$\psi_{n,l,m} = \sqrt{\frac{1}{\pi a_0^3}} e^{-r/a_0}$$

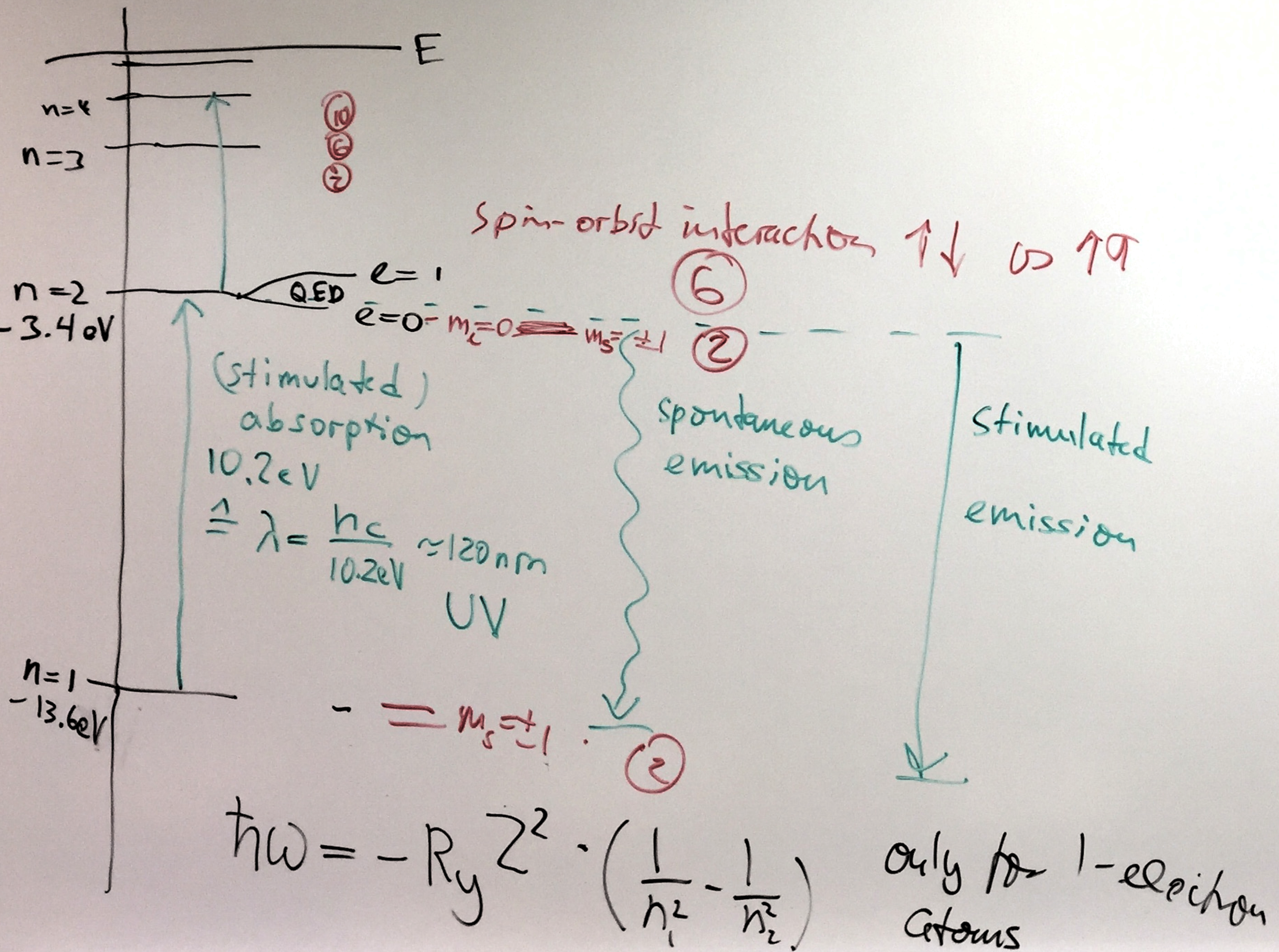
$n=1, 2, \dots$ $l=0, 1, \dots, n-1$ $m=0, \pm 1, \pm 2, \dots, \pm l$

$$a'_0 = a_0 \cdot \frac{m_e}{\mu Z}$$

Q.N. \rightarrow Q. Field Theory

Q.E.D. example \uparrow = interaction of photons + charges

Photon: $E = \hbar\omega$



Spin S
vs. Orbital ang. mom. L

electron: $s = \frac{1}{2}$

$$\vec{S} |\psi_{\text{electron}}\rangle = \frac{\hbar}{2} \cdot \frac{3}{4} |\psi_{\text{electron}}\rangle$$

$$S_z |\psi_{\text{electron}}\rangle = \hbar m_s |\psi_{\text{electron}}\rangle$$

$$m_s = \pm \frac{1}{2}$$