

Now for something totally (?) different...

- OUR FIRST REAL FORCE LAW: $\mathbf{F} = -G m M / r^2$
 - Universal gravitational force (Newton)
 - Acting between any two masses
 - Proportional to both of these masses
 - Inversely proportional to the square of their distance
 - Always attractive: $m, M > 0 \Rightarrow \mathbf{F}$ is negative - tends to reduce r

- NOW: Electrostatic force (Coulomb):

- Acting between any two charges Q, q
- Proportional to both of these charges
- Inversely proportional to the square of their distance
- Sign of force depends on relative sign of charges;
can be both attractive (opposite sign) or repulsive (equal sign)

$$F = +k \frac{Qq}{r^2}$$

What are charges?

- Charge is a fundamental property of matter
 - Measured in units of Coulomb (C) - $1\text{ C} = 1\text{ A} \times 1\text{ s}$
- Most elementary particles are charged
 - Charge is **quantized**: all charges are multiples of $e = 1.61 \cdot 10^{-19}\text{ C}$ *)
- Comes in TWO kinds: + or -
 - Equal sign charges repel each other, opposite sign charges attract
- Total charge (sum of all “+” minus all “-”) never changes - charges cannot be created or destroyed, only moved around or “neutralized” (*Charge conservation*)

*) Except quarks which have charges of $\pm \frac{1}{3} e$ or $\pm \frac{2}{3} e$ **)

**) But in any elementary particle reaction charges change only by integer multiples of e

Coulomb's Law

$$F = k \frac{Qq}{r^2}$$

- Measure each charge in Coulomb
- Measure r in m
- Measure force in N
- $\Rightarrow k = 9 \cdot 10^9$! [Nm²/C²]
- NOTE: 1kg of protons = $6 \cdot 10^{26}$ protons = 100,000,000 C! \Rightarrow Force between two 1kg-bags of protons 1 m apart = $9 \cdot 10^{25}$ N !!
- GRAVITATIONAL force between those same two bags is $6.7 \cdot 10^{-11}$ N - 36 orders of magnitude less!!!

Huh?

- Because Coulomb forces are so tremendous, and...
- Because there are both positive and negative charges,
- and because like charges repel and opposite charges attract
- -> charges are nearly always nearly perfectly balanced.
 - Example: Atom, matter in the Universe
- Coulomb forces simply add (*Principle of Superposition*), so positive and negative charges cancel each other out
- Small amounts of charges can be transferred fairly easily from one object to another (typically μC or less)
 - Example: Shuffling over a carpet, combing a cat,...
 - Photocopier, laser printer, plastic wrap,...

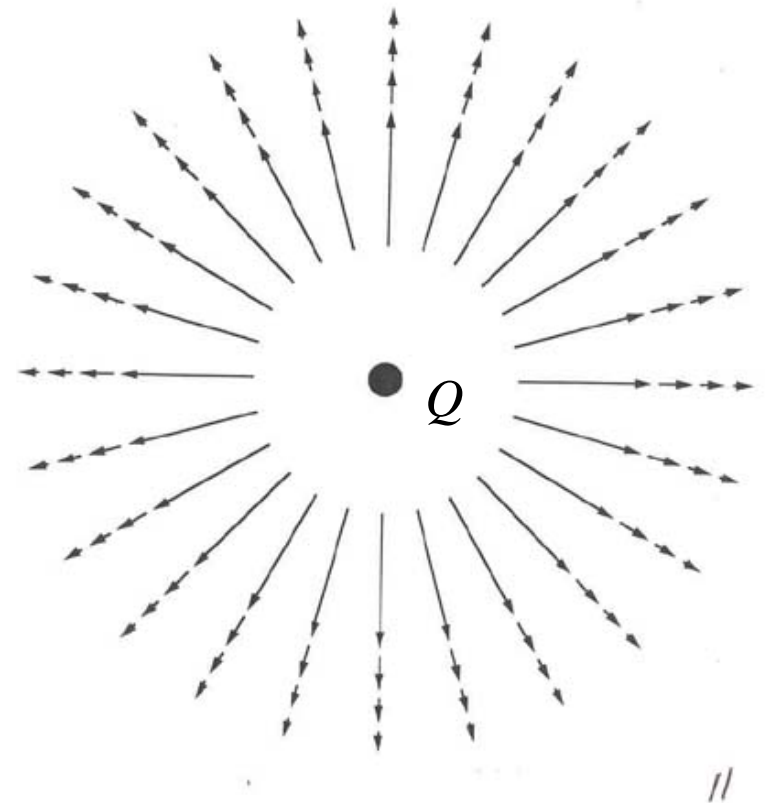
Moving charges around

- Two (or more) different types of materials in everyday life:
- Conductors
 - Huge amounts of charges (usually electrons) can move around easily:
 - Can shield other charges; charges tend to even out quickly
 - Can induce charges
 - Can transfer charges
 - Examples: All metals, plasma, sea water,...
 - Most perfect example: Superconductors
- Insulators
 - Charges are “stuck” - can keep charges in place (except for small transfers from surface to surface – shuffling, rubbing,...)
 - BUT: can induce “polarization” (e.g. balloons stuck to ceiling)
- ...and semiconductors (in transistors, computer chips etc.)

Electric Field

$$F = k \frac{Qq}{r^2}$$

- Coulomb's Law tells us what force a charge Q would exert on charge q if charge q sits at \mathbf{r} - see Fig.
- But the electric properties of Q don't depend on whether we measure the force on q or not
- \Rightarrow Concept of a FIELD: An intrinsic property of ALL OF SPACE due to some agent
- Make electrostatic force a two-step process: First charge Q generates a field $E = kQ/r^2$, second charge q interacts with that field: $F = qE$



Is it “real”?

- Can be used to calculate the behavior of a complicated arrangement of charges: First calculate the field \mathbf{E} it produces, then you’ll know what force it will exert on any “test” charge q that you put somewhere into this field: $\mathbf{F} = q\mathbf{E}$
(**Note:** force is proportional to q and points in the SAME direction as \mathbf{E} if q is positive; else in the opposite direction!)
- Can be used to describe how CHANGES in the distribution of charges propagate (at most with speed of light -> Einstein)
- Can carry energy (charged up capacitor, electromagnetic wave)
- Can even carry “mass” (via Einstein’s $m = E/c^2$)
- On fundamental (quantum mechanical) level, is associated with a “real” particle: the photon.

How to visualize?

- Draw field lines: Starting at “+” charges, ending at “-” charges (or going on forever)
 - The bigger the charge, the more field lines start (end) at it
 - Point in the direction of the field at each point
 - Spread out evenly
 - Never cross
 - Example: Hair standing up
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- Surprise: “automatically” give the correct STRENGTH of the field as well: proportional to DENSITY of field lines

Revisit

- Conductors in electric fields
 - Huge amounts of charges can move around easily:
 - Shields outside electric fields completely on the inside *)
 - All charges sit on the outside
 - Keep safe inside cars during thunderstorms
 - => Conductors are attracted to charged objects
- Insulators in electric fields
 - Charges are “stuck” - can’t completely shield outside electric fields
 - BUT: can induce polarization -> outside electric fields will be weakened inside (e.g.: Water or oil will weaken the field to 1/100 or less)
 - Polar molecule align themselves with the electric field so that the negative sides are closer to the source of the field lines
 - => Insulators are attracted to charged objects!

*) as long as no currents are flowing

Potential energy in Electrostatics

- Electric field \mathbf{E} (e.g., due to a positive charge Q) times amount of (test) charge q : Force \mathbf{F}
- Move charge q towards charge Q (against field direction): Need to do work if q is positive, get work out if q is negative!
- This work can be retrieved by letting go of q - it will accelerate (-> kinetic energy from stored potential energy)
- Work only depends on initial and final position -> CONSERVATIVE FORCE
- Can define electrostatic potential energy $U_{\text{pot}}^{\text{elec}}$ of charge q (in presence of charge Q):
 - Larger if $|q|$ increases
 - positive if q is positive, negative otherwise
- Can store energy in electric devices (like vdGG, capacitor, battery) by storing charges at a high electrostatic potential energy
- Example: Electrostatic potential energy for q in field of point charge Q :
Similar as for gravitational potential energy...

$$U_{\text{pot}}^{\text{elec}} = k \frac{qQ}{r}$$

Electric POTENTIAL

- Since potential ENERGY is proportional to q , can define electric POTENTIAL U (= “voltage”) at every point: equal to potential ENERGY that q would have at that point, divided by q .
- Similar to electric field: electric potential becomes a function of point in space alone (once the charge distribution creating it is known)
- Unit: J/C = V
- Potential due to a single point charge Q : $V_{pot} = k \frac{Q}{r}$
- Very important practically: Batteries, household outlets, transmission lines, charged up objects...
- Remember: Energy stored = Voltage x charge

$$\begin{array}{ccc}
 \mathbf{E} & \xrightarrow{\text{over some distance } d} & V = \mathbf{E}d \\
 \text{times } \downarrow q & & \text{times } \downarrow q \\
 \mathbf{F} & \xrightarrow{\text{over some distance } d} & U_{pot} = \mathbf{F}d
 \end{array}$$