# **Computational Physics**

Physics 811 has the task of both giving a solid treatment of basic methods, tools, and techniques of computational physics used in modern physics, and developing skills for practical solving computational problems in physics.

This is not a course in computing science, or in programming. It focuses specifically on practical methods for solving physics problems. The course is therefore designed such that a significant fraction of the students' time is spent actually programming specific physical problems. In this course the students *learn by doing*. Students will practice writing, compiling, and running computer programs, together with analysis of results, and presentation of their results as scientific reports

**University Catalog** Physics 811 – CRN 19526. Computational Physics. Lecture 3 hours; 3 credits.

Studies of high level computer languages. Computational techniques used in physics. Numerical techniques for differential and integral problems. Algebraic processing languages. Introduction to scientific visualization techniques.

Prerequisite Students are expected to be familiar with at least one programming language

(Fortran, C, C++, Basic, or Java).

**Instructor** Dr. Alexander Godunov

Office: OCNPS 0219 (Oceanography and Physics)

Phone: 683-5805 agodunov@odu.edu

Web page: http://www.odu.edu/~agodunov/teaching/phys811\_09

Classes Tuesday, Thursday 13:30 – 14:45 (lectures)

Oceanography & Physics, Room 303

Office Hours Tuesday 11:30 – 12:30 (office), 16:00 – 17:00 (the Physics Learning Center),

Thursday 11:30 – 12:30 (office),

and by appointment

Materials (recommended)

There is no a single book that could serve as a textbook for the course. Therefore most material is presented in the lecture notes, available from the web page -

http://www.odu.edu/~agodunov/teaching/notes/index.html

Besides, following books can be helpful (if you can find one in a library)

Computational Physics: Problem Solving with Computers, by R. H. Landau and M. J. P. Mejia, John Wiley & Sons (1997); A Survey of Computational Physics by R.H. Landau, M. J. Paez and C. C. Bordeianu, Princeton University Press (2008). Introductory Computational Physics by A. Klein and A. Godunov, Cambridge

University Press (2006)

An Introduction to Computer Simulation Methods: Applications to Physical Systems (3rd Edition) by Harvey Gould, Jan Tobochnik, Wolfgang Christian,

Addison Wesley (2006)

Computation In Modern Physics, by W.R. Gibbs, World Scientific (2006)

Physics By Computer, W. Kinzel and G. Reents, Springer (1998)

Numerical Methods for Engineers and Scientists by Joe D. Hoffman. 2<sup>nd</sup> Edition,

Marcel Dekker, Inc. (2001)

#### Course structure

Different people learn in different ways. Therefore this course offers a learning environment with a diversified set of options that you can tailor to your individual learning style. There are class meetings, homework assignments, computational projects, and practice. There are many ways to get assistance with the material in this course: the office hours, appointments, e-mail, phone

#### **Keys to success**

Right motivation, working diligently, effectively and efficiently is the key to success. If you work regularly and allocate enough time each day to practice and complete the assignments on time and keep up with the course, you will get the most out of the course both intellectually and grade-wise.

You should invest about 6-9 hours per week outside of class to succeed in this course. This is consistent with university guidelines (i.e. two to three hours of outside preparation time for every credit hour). Students with little or no programming experience (or those who love the subject and wish to do extremely well in it) may want to put in more hours. Please, let me know as soon as possible if you have difficulties and may need extra help.

You are recommended to start you assignments well before the last night when your assignments are due. It is a general experience that a computer program usually does not work correctly (if works at all) at the beginning. A search for a problem, or a computer bug, may take more time that you expect.

#### Homework

Doing the homework problems is one of the best ways to learn the art of computational physics. Credit for homework is given to encourage practicing and thinking about computational physics on a regular basis. This credit influences the final grade for this course. Assignments may be submitted early but will not be accepted late.

## **Projects**

There will be midterm computational projects and one final project. The projects will aim to solve specific problems in physics. You will be required to submit a report on each project. All reports should have the following sections: title, description of the problem, equations and computational model, testing, example of input parameters, results (figures, tables, analysis), and conclusion.

The report and your computer program should be submitted electronically by the due date and time (as an attachment, including an example with input/output files) to agodunov@odu.edu. This will enable the assessors to check and run your program if necessary. Please, remember that "no submitted program = no credit for the assignment". Recommended formats for reports are MSWord and PDF, with all figures embedded in the body of the document.

I would appreciate getting a carbon copy of your report as well.

Each assignment will be graded for completeness and correctness. Clarity of your presentation may affect your grade.

No make-up projects will be given. In case you have a legitimate reason for missing a project deadline, consult with me before, or within 24 hours after the deadline.

Regrade: Requests for correction of grading mistakes on projects can be made when the work is returned to you. The requests must be made within three days after getting your grade. Regrade requests should be written. In their request, students must explain why they believe there is a mistake in grading and why they deserve more credit. It is not a plea for more points

Physics 811

**Exams** 

Since this is a laboratory like course there will be no traditional exams but midterm projects, and one final project. The final exam will consist of an oral presentation of the final project and an accompanying written paper (in the format of a research article).

The final examination is mandatory and will be given only at the scheduled time.

Grades

The final grade is calculated on an absolute scale. There are 100 points possible for this course of which

30 points are for homework assignments,

50 points for midterm projects

20 points for the final project and examination.

A letter grade is determined only at the end of the term.

Grade forgiveness policy: assignments (homework, projects) handed in late without an excuse will be pro-rated as followed: 90% up to 24 hours late; 80% up to 48 hours late; 50% thereafter until the last day of class.

**Attendance** 

Attendance in lectures is optional; however, you are responsible for all information discussed in class, including any announcements.

Collaboration

Collaboration is strongly encouraged. Because the course is graded on an absolute scale, you will never reduce your grade by helping others — on the contrary, by doing so you will reinforce your own knowledge and improve your performance.

Activities for which collaboration is encouraged: group projects, understanding issues discussed in class, using compilers and other software, using numerical libraries.

Activities for which collaboration is NOT permitted are: homework assignments, individual projects and the final examination.

Professional Conduct

In Physics 811 high professional standards, including ethical standards, are promoted. Plagiarism and cheating are serious offenses and may be punished by failure in the course. The academic integrity code is to be maintained at all times.

## **Tentative Course Outline**

## Part 1: Introduction to computing

- 1. Introduction (What is computational physics?)
- 2. Tools of computational physics
- 3. Short introduction to C/C++
- 4. Short introduction to Fortran 90/95

## Part 2: Basic numerical methods with applications to physics

- Interpolation: linear and polynomial interpolation, divided difference polynomials, equidistant points -Newton's forward/backward difference, spline interpolation
- 2. Derivatives: Lagrange polynomials, Newton difference polynomials, finite difference approximations
- Numerical integration: simple quadratures (trapezoid, Simpson), Newton-Cotes formulas using divided difference polynomials, Gauss quadratures, integration with adaptive step size, special cases (oscillating functions, improper integrals, singularities, multiple integrals)
- Solution of non-linear equations: closed domain methods (bisection and regula falsi), open domain methods (the Newton's method, the secant method), nonlinear systems of equations (the Newton's method)
- 5. Ordinary differential equations
  - 5.1 Initial value problems: the first-order Euler method, the second-order single point methods (predictor-corrector, leap-frog, Verlet), Runge-Kutta methods, adaptive methods, extrapolation methods, multipoint methods, stiff ODEs
  - 5.2 boundary value problems: the shooting method, the equilibrium method, the Numerov's method eigenvalue problems: the equilibrium method
- 6. Systems of linear algebraic equations
  - 6.1 Direct elimination methods: simple direct elimination, Gauss elimination (pivoting, scaling), Gauss-Jordan, LU factorization, determinants, tri-diagonal systems (Thomas method), condition numbers
  - 6.2 Iterative methods: Jacobi iteration, Gauss-Seidel, successive over-relaxation (SOR)
  - 6.3 Eigenvalue problem: the direct power methods, Jacobi method (the QR method, the Householder, the Faddeev-Leverrier, the Lanczos method)
- 7. Partial Differential Equations
  - 7.1 Elliptic PDE: the finite difference method, iterative methods
  - 7.2 Parabolic PDE: finite difference grid, the Richardson (leap-frog method), the DuFort-Frankel method, the Crank-Nicolson method
  - 7.3 Hyperbolic PDE: the forward-time centered space methods, the Lax methods, the upwind method.
- 8. Fourier transforms: discrete Fourier transforms, fast Fourier transforms

## Part 3: Application to physics & Computer simulation methods

- 1. Classical mechanics
  - 1.1 Projectile and particle motion
  - 1.2 Classical scattering
  - 1.3 Few body problems

#### Monte Carlo simulation

Random numbers (generators, uniform and non-uniform distributions), Monte Carlo integration, Metropolis algorithm, random walk (unrestricted, restricted, persistent, self-avoiding).

- 3. Quantum Mechanics
  - 3.1 1D Schrödinger time-independent equation (eigenvalues)
  - 3.2 quantum scattering on a spherically symmetric potential.
  - 3.3 1D time-dependent Schrödinger equation
- 4. Chaos: Poincare maps, physics pendulum, the butterfly effect.
- 5. Critical mass problem.
- 6. Data fitting and analysis: least squares method, linear and non-linear functions
- 7. Molecular dynamic simulation
- 8. Cellular automata.

## Part 4. Scientific software

- 1. Introduction to scientific software (Maple, MathCad, Mathematica)
- 2. Plotting and visualization software
- 3. Libraries of numerical methods
- 4. Libraries of physics programs
- 5. High-performance computing